## Mark schemes

1. (a) MAX 2

Uncertainty in one/each reading is $1 \mathrm{~mm}{ }_{1} \checkmark$
Allow the uncertainty in (reading) the position of a spot is 1 mm .
OR
The measurement involves making two readings / there are two uncertainties (to be considered) in this measurement ${ }_{1} \checkmark$

Owtte
Difficulty / uncertainty in locating (exact) position of (centre of) spot $2 \checkmark$
Or
Difficulty / uncertainty in lining up the (centre of the) spot with a graduation on the ruler ${ }_{2} \sqrt{ }$

Or
Difficulty / uncertainty in locating the position of $A / B{ }_{2} \sqrt{ }$
Do not allow:

- because the smallest division is 1 mm
- hard to see measurements to less than 1 mm (need to link to position of spot (or A or B)
- "because of both sides of the ruler" on its own
- "ruler slightly misaligned" too vague
the uncertainties from two (readings) are added $3 \checkmark$ insufficient includes:
- uncertainty doubles
- uncertainty is twice the smallest division
- Random error or human error or error without further detail.

However:
The uncertainty doubles because there are two readings scores MP1
Also:
The uncertainty doubles because there are two readings with identical uncertainties would score 2 marks.
Mention of range of repeated measurements $\div 2$ is not applicable in this case.
(b) (Adds the uncertainties $=)_{4}(\mathrm{~mm})_{1} \checkmark$

Or
Use of by substitution
(percentage uncertainty=) $\frac{\text { uncertainty }}{\text { value }}(\times 100)(\%)_{1} \checkmark$
(\% uncertainty =) 0.74 or 0.7 (c.a.o) ${ }_{2} \sqrt{ }$ ( 1 or 2 significant figures only)
$1^{\text {st }}$ mark
Expect to see:
(percentage uncertainty $=) \frac{4}{544}(\times 100)(\%)$
Maximum 1 mark for
Condone (in substitution):

- $2 / 289,2 / 255,2 / 272,2 / 544,4 / 289,4 / 255,4 / 272$
- power of ten errors (POT errors)
- must be a recognisable uncertainty

Maximum 1 mark for
use of
(percentage uncertainty $=) \frac{\text { uncertainty }}{\text { mean (value) }}($ value $)(\times 100)(\%)$
along with substitutions of

- $\quad 2 / 289,2 / 255,2 / 272,2 / 544,4 / 289,4 / 255,4 / 272,4 / 544$
- power of ten errors
condone for 1 mark
$((2 / 289+2 / 255) \times 100=)$
$1.48 \%$ or $1.5 \%$
$2^{\text {nd }}$ mark
Condone working leading to 2nd mark for:
Use of (percentage uncertainty=) $\frac{2}{272}$
Do not allow mean of two separate \% uncertainties or incorrect formula quoted and used in workings
(c) MAX 2

The percentage uncertainty in $c$ is smaller than for $a$ or $b$ because $c$ has a larger value (than a or b separately) ${ }_{1} \downarrow$
or \% uncertainty in c is half the percentage uncertainty in $\mathrm{a}+\mathrm{b} \boldsymbol{1} \checkmark$
or The percentage uncertainty in c is smaller because its uncertainty is smaller for the same data value ${ }_{1} \checkmark$

Insufficient:

- $\quad c$ has a smaller uncertainty
- $\quad a+b$ has a larger uncertainty
- $\quad$ The uncertainty of $a+b$ is combined
$c ' s(\%$ uncertainty $=) 0.37$ or $0.4{ }_{2} \sqrt{ }$ or $c ' s(\%$ uncertainty $=) \frac{2}{544} \times 100{ }_{2} \sqrt{ }$
idea that $c$ s measurement involves fewer readings than the sum of a and $\mathrm{b}_{3} \checkmark$ or
idea that c requires fewer measurements than the sum of a and $\mathrm{b}_{3} \checkmark$
Accept converse
Where numbers are quoted, these must be consistent with terms used.
4 readings, 2 readings
2 measurements, 1 measurement
(d) (when laser is switched on) always stand behind the laser (unless taking readings) $\checkmark$

Or
if in front of laser (when switched on) look away from the laser (eg when taking readings) $\checkmark$

Or
if in front of laser (when switched on) don't look at/towards the laser (eg when taking readings) $\checkmark$

Or
don't look directly into the laser (beam) $\checkmark$
Or
direct laser towards nearest wall $\checkmark$
Or
switch off laser when not in use $\checkmark$
Or
ensure (glass) reflective surfaces are covered (prevent reflections) $\checkmark$

Or
Do not shine the laser onto a reflective surface $\checkmark$
Or
place safety notices outside the laboratory [room] $\checkmark$
Or
don't shine laser at eye level $\checkmark$
Or
mark positions with pen/pencil and measure after laser switched off $\checkmark$
Or
laboratory is normally illuminated (not darkened) $\checkmark$
Where a list of safety measures has been given:

- Treat more than one correct as neutral
- Penalise incorrect safety measure in a list that may include correct safety measures.
Do not credit weak statements:
- Do not look at the laser
- Don't point the laser anywhere except at the grating
- Don't look directly at the laser

Beware of references to "the light".
(e) $\quad\left(\tan \theta=\frac{0.544}{1.280}=\theta=\right) 23.0\left(^{\circ}\right) \checkmark$
allow 2 or more significant figure answer
acceptable common answers:
23, 23.0, 23.03, 23.025, 23.0255
Where more than 3 sf quoted, the number must be correct.
alternative method
(valid attempt to determine distance from grating to spot $\boldsymbol{E}$, eg
$\left(\right.$ distance $\left.=\left(\sqrt{0.544^{2}+1.280^{2}}\right)=1.391\right)$
$\left(\sin \theta=\frac{0.544}{1.391}=0.391\right)$
( $\theta=$ ) 23.0 $\left(^{\circ}\right.$ ) $\checkmark$
allow 2 or more significant figure answer
acceptable common answers:
23, 23.0, 23.03, 23.025, 23.0255
Condone mid-calculation rounding leading to errors in 4th sf where quoted.
(f) use of $n \lambda=d \sin \theta_{1} \checkmark$
or
(if nothing else seen) $\mathrm{d}=3.3 \times 10^{-6} \mathrm{~m}, \checkmark$
Use of:
Correct rearrangement where subject would be $\lambda$
or correct substitution of $n, d$ and $\theta$
Expect to see $n=2, d=3.3(3) \times 10^{-6}, \theta=23(.0)$
Condone one error in substitution for $n$ or $d$ in a correctly rearranged equation where subject would be $\lambda$
(or where answer indicates the correct working for incorrect
numbers, $d$ error leads to $5.86 \times 10^{4}$ )
Condone power of ten errors in working
$\lambda=6.5(2) \times 10^{-7}(\mathrm{~m})_{2} \sqrt{ } \mathrm{ecf}$
2 or 3 sf only
where 3 sf quoted answer must be in range 651 to 652 nm (or ecf)
Common ecf (sin $\theta$ error in 1.5):
Expect to see an answer that rounds to $7.1 \times 10^{-7} \mathrm{~m}$ to 2 sf
(g) The second mark $(2 \sqrt{ })$ is contingent on the award of the first mark $(\sqrt{ } \sqrt{ })$.

Increase distance from grating to screen / increase y ${ }_{1} \checkmark$
(This will increase distance $y$ (and/or c) therefore) decreasing the percentage uncertainty in $\mathrm{y} / \mathrm{c} /$ fringe spacing $/ \theta / \sin \theta_{2} \checkmark$

Do not accept:

- darkened room
- use a (vernier) caliper
- use a travelling microscope
- Repeat
- Repeat and average
- Computer/data logger/camera
- Ruler with smaller divisions
- Make the maxima further apart (details on how this is achieved are required)
- Increase distance between laser and screen.

Decreases the percentage uncertainty in $y_{2} \sqrt{ }$

Or
Use a higher-order spot ${ }_{1} \checkmark$
(This will increase distance from centre spot to higher-order spot therefore) decreasing the percentage uncertainty in the fringe spacing $/ \theta / \sin \theta_{2} \checkmark$

Condone reference to this distance as $c$
Or
Measure distance between $A$ and $E_{1} \checkmark$
(This increases the distance therefore) decreasing the percentage uncertainty in $\mathrm{c}_{2} \checkmark$ No details of determination of c are required.
3. (a) general procedure

- collect water for a measured time;
- divide measured / calculated volume by time to determine rate ${ }_{1} \checkmark$
static volume should be measured after timing, eg
reject 'measure time to fill cylinder' or ${ }_{1} \checkmark=0$
accept 'find $V$ for different $t$, plot $V$ against $t$,
gradient $=$ Q' but not if by continuous flow method
names 2 suitable instruments ${ }_{2} \sqrt{ }$
for time use stopwatch or stopclock;
treat as neutral: 'timer' or 'light gate / data logger'
for volume use measuring cylinder / graduated beaker;
treat as neutral: 'measuring beaker'/ 'burette'
OR
for mass use balance; use of $V=\frac{m}{\rho}$ (any subject)
condone 'volume of 1 g is $1 \mathrm{~cm}^{3}$;
reject 'weigh'/weighed'
method to reduce uncertainty in volume ${ }_{3} \checkmark$ read water level at bottom of the meniscus (or wtte or allow sketch); don't penalise further use of 'beaker' treat as neutral: 'dry cylinder before use'
OR
procedure to avoid systematic error in determining mass, eg tare / reset / zero the balance with empty beaker on pan / find mass of beaker empty and subtract from mass of beaker plus water;
don't penalise further use of 'weigh'/ 'scales' allow 'use balance on a horizontal surface'
method to reduce uncertainty in time ${ }_{4} \checkmark$
$\checkmark$ ensure stopwatch is zeroed / reset before use
added detail ${ }_{5} \sqrt{6}{ }_{6} \checkmark{ }_{7} \checkmark$
collect large(r) volume / for long(er) time $/ \geq 60 s_{5} \checkmark$
this reduces percentage / fractional uncertainty ${ }_{6} \checkmark$ read at eye level or wtte, to reduce parallax $7 \checkmark$
(b) sensible mark identifying second box indicating ( $\mathrm{N} \mathrm{m}^{-2} \mathrm{~s}$ ) only


## auto marked question

(d) appropriate use (ie close to and parallel with the vertical side of the tube, but not necessarily in contact with the tube) of:
a metre ruler made vertical using a set-square in contact with the bench / floor / (flat) surface

OR
a plumb line / weight on vertical string (reject 'pendulum')

OR
a spirit level $\checkmark$
the mark can be awarded for a convincing sketch, eg use of a very large set square without ruler
accept 'tri-square' for set square
the only acceptable horizontal reference is the bench: don't allow use of horizontal T, eg set square placed on T even if sketch looks convincing
no credit for attempt to show graduations on tube are horizontal / use of 'protractor' for set-square / 'each side of meniscus at same level'/ use of clamp stand rod or wall as vertical reference
(e) attempted use of $y=y_{0} \mathrm{e}^{-\lambda \Delta t}$ with substitution of values of $y, y_{0}$ and $\Delta t$ obtained directly from Figure 4 / plausible values obtained from Figure 7

OR
tangent drawn on Figure 4 to find $\frac{d y}{d t}$;
use of $\frac{d y}{d t}=(-) \lambda \times y^{*}$ and $y^{*}$ is where tangent meets the curve ${ }_{1} \checkmark$
valid calculation seen leading to a result for $\lambda$ that rounds to 3 sf in range 4.45 to 4.55 $\times 10^{-3}\left(\mathrm{~s}^{-1}\right)$;
award if seen in body of answer ${ }_{2} \sqrt{ }$
for ${ }_{1} \checkmark$ do not penalise $y / y_{0}$ interchanged, read off
errors, manipulation errors $/ \Delta t=t / t 0 / \frac{t}{t_{0}}$ or use of incorrect
symbols eg $A, N$ for $y$;
no ecf for ${ }_{2} \sqrt{ }$
allow use of Figure 7
$y_{0}=60.0 \mathrm{~cm}, y=52.2 \mathrm{~cm} ; \Delta t=60-29=31 \mathrm{~s}$
$52.2=60 e^{-31 \lambda} ; \therefore \lambda=4.49 \times 10^{-3} \mathrm{~s}^{-1}$
if the intermediate step is seen, eg

$$
\lambda=\frac{1}{\Delta t} \times \ln \left(\frac{y_{0}}{y}\right)=\frac{1}{31} \times \ln \left(\frac{60}{52.2}\right)
$$

accept 'log' for ' $1 n$ '
no credit allowed for reverse-working method in a 'Show that' problem
no credit for assuming straight line and $y=m x+c$, measuring the gradient then by determining the
equation of the line or by using $m=\frac{y_{2}-y_{1}}{t_{2}-t_{1}}$
determines the half life; finds $\lambda$ from $\frac{\ln 2}{\text { half life }}$
no credit for common error $\lambda=$ gradient $\times 2$
for ${ }_{2} \sqrt{ }$ look for any answer in the body that deserves credit (for a 'Show that' we can overlook truncation in the value given on the answer line)
variation on use of use of $y=y_{0} e^{-\lambda \Delta t}$ for ${ }_{1} \sqrt{ }$ :
$\lambda$ can be found if points $t_{1}, y_{1}$ and $t_{2}, y_{2}$ are used and the values substituted into $\frac{y_{1}}{e^{-\lambda t_{1}}}=\frac{y_{2}}{e^{-\lambda t_{2}}}$;
if this approach is used substitute the data into $\lambda=\frac{1}{\Delta t} \times \ln \left(\frac{y_{0}}{y}\right)$ to confirm that the result for $\lambda$ is correct before awarding ${ }_{2} \sqrt{ }$
(f) use of $T_{y / 2}=\frac{\ln 2}{\lambda}$ OR $\frac{\ln 0.5}{-\lambda}$ with substitution of recognisable $\lambda$;
evaluated to $\geq 2$ sf in range 140 s to $170 \mathrm{~s} \checkmark$ calculation can have any subject; accept use of 2 sf $\lambda=4.5 \times 10^{-3}$ usually leading to 154 but allow correctly truncated to 150 or $1.5 \times 10^{2}$
(g) (mostly) continuous line drawn on Figure 7;
below dashed line and with negative gradient between $t=0$ and $t=120$;
do not penalise linear line or shaky / thick / hairy line or slight
discontinuities; accept $\approx$ horizontal after 100 s $_{1} \checkmark$
line passes through:

| $t / \mathrm{s}$ | $y / \mathrm{cm}$ |  |
| :---: | :---: | :---: |
|  | $\min$ | $\max$ |
| 0 | 33 | 35 |

AND through EITHER of

| $t / \mathrm{s}$ | $y / \mathrm{cm}$ |  |  |
| :---: | :---: | :---: | :---: |
|  | $\min$ | $\max$ |  |
| 60 | 24 | 28 |  |
| 120 | 17 | 23 | ${ }_{2}$ |


4. B
5. (a) to reduce the impact of systematic error: tare [zero] the callipers before use OR
take reading with callipers fully closed (at some stage) and subtract from readings ${ }_{1} \checkmark$
to reduce the impact of random error: take measurement several times for different diameters/directions and calculate mean
OR
take measurement several times for different diameters to check for anomalies ${ }_{2} \sqrt{ }$
(b) use of inside jaws on callipers required: must have a clear drawing with inside jaws in contact internal diameter ${ }_{1} \checkmark$


A sectional view of the magnet must be given
Jaws must be inside cavity (as here)
(c) Determines a cross-sectional area: (larger $\mathrm{A}=) 2.82$
$\times 10^{-3}$ or $($ smaller area $=) 2.932 \times 10^{-4}$

## OR

states that the cross sectional area from $\Delta$
$A=\left(\frac{\pi D^{2}}{4}-\frac{\pi d^{2}}{4}\right)$

## OR

Calculates one volume correctly ${ }_{1} \checkmark$
Allow POT error ${ }_{1} \sqrt{ }$ and ${ }_{2} \sqrt{ }$
Where $r$ is used must have an additional statement on how r relates to $D$ (in the case where there is no correct substitution and no correct answer)
substitution of $D=59.90, d=19.32$ and $t=12.09$ into
$V=\left(\frac{\pi D^{2}}{4}-\frac{\pi d^{2}}{4}\right) \times t$

## OR

$$
V=\text { their } \Delta A \times 12.09
$$

## OR

Correctly finds difference in their volumes ${ }_{2} \sqrt{ }$
Or equivalent
Correct substitution into
$V=\left(\frac{\pi D^{2}}{4}-\frac{\pi d^{2}}{4}\right) \times t$
receives the first two marks (allow POT)
Expect values:
$V_{D}=3.41 \times 10^{-5}\left(\mathrm{~m}^{3}\right)$
$V_{d}=3.54 \times 10^{-6}\left(\mathrm{~m}^{3}\right)$
$3.1 \times 10^{-5} / 3.05 \times 10^{-5} / 3.053 \times 10^{-5}\left(\mathrm{~m}^{3}\right)_{3} \checkmark$
no limit on maximum sf
Correct answer scores 3
Allow 3rd sf round error where
answer rounds to $3.1 \times 10^{-5}$
when correct method seen

## (d) Procedure:

## MAX 2

Take more measurement(s) of $h$ for additional / different masses (of clay) $\checkmark$ More than one added mass, allow varies amount of clay

Convert (total) mass into weight (and equal to the repulsive force of magnet $\mathbf{A}$ on magnet B) $\checkmark$

Describe method to measure $h$ using ruler or set square $\checkmark$
(in this case determination of $k$ must be consistent with graph)

## Analysis:

Plot a graph of $F$ against $1 / h^{3} \checkmark$
Condone $1 / h^{3}$ against $F$ or equivalent
Should be a straight line of best fit $\checkmark$
This mark can be awarded if seen by drawing of straight line with positive gradient on sketch of graph

## Determination of $\boldsymbol{k}$ :

## MAX 1

Measure gradient and set equal to $k \checkmark$
Allow one mark for plot of $F$ against $h^{3}$ and statement that area under graph is $k$. Mark Procedure as scheme

Substitute (total) weight into formula and rearrange to find $k \checkmark$
Must be consistent with graph
6. (a) path difference for two waves $\checkmark$

Allow 'waves travel different distances' Condone out of phase
gives rise to a phase difference $\checkmark$
if phase and path confused only give 1 for first 2 marks
Destructive interference occurs $\checkmark$ allow explanation of interference
(b) (Path difference $=) 0.056 \mathrm{~m} \checkmark$

Path difference $=2 \lambda$ or wavelength $=0.028 \mathrm{~m} \sqrt{ }$
Use of $f=c / \lambda$ so $f=11(10.7) \times 10^{9} \mathrm{~Hz} \checkmark$
Allow 2 max for $5.4 \times 10^{9} \mathrm{~Hz}$ or $2.7 \times 10^{9} \mathrm{~Hz}$
Allow ecf
(c) Intensity decreases with distance $\sqrt{ }$

One wave travels further than the other $\checkmark$
Amplitudes/intensities of the waves at the minimum points are not equal $\sqrt{ }$

Or "do not cancel out"
$\max 2$
(d) The signal decreases/becomes zero $\checkmark$

The waves transmitted are polarised $\checkmark$
zero when detector at $90^{\circ}$ to the transmitting aerial/direction of polarisation of wave $\checkmark$
$\max 3$
7. (a) Both $t_{\mathrm{m}}$ values correct: $0.404,0.429$

AND
Both $t_{\mathrm{m}}{ }^{2}$ values correct: $0.163,0.184 \checkmark$ Exact values required for the mark.
(b) Both plotted points to nearest $\mathrm{mm} \checkmark$

Best line of fit to points $\checkmark$
The line should be a straight line with approximately an equal number of points on either side of the line.
(c) Large triangle drawn (at least $8 \mathrm{~cm} \times 8 \mathrm{~cm}$ ) $\checkmark$

Correct values read from graph $\checkmark$
Gradient value in range 0.190 to $0.222 \checkmark$
Allow 2 or 3 sf for gradient
(d) $\quad g=9.71\left(\mathrm{~ms}^{-2}\right)$ or correct value from gradient value in (c) $\checkmark$.
(The answer must be in the range 9.0 to $10.5\left(\mathrm{~ms}^{-2}\right)$ ).
Allow 2 or 3 sf.
Unit not required
(e) $\%$ difference $=\frac{(9.81-9.71)}{9.81} \times 100=1.02$

OR correct computation using value from (d) $\checkmark$
If the candidate's value is exactly 9.81, then a statement that there is no (or zero) percentage difference is acceptable.
No sf penalty.
NB. Allow an answer from a calculation with either the candidate's value or the accepted value as the denominator in the equation.
(f) $0.001 \mathrm{~s} \sqrt{ }$ (half the spread)
(Must have unit).
(g) $\quad g=2 s / t_{m}^{2} \checkmark$
$=2 \times 0.300 / 0.245^{2} \checkmark$
$=10.0$ (or 10.00 ) $\mathrm{ms}^{-2} \checkmark$
Unit required and 3 or 4sf for the last mark.
(h) \% uncertainty in $s=0.33$ and
$\%$ uncertainty in $t_{\mathrm{m}}=0.41 \checkmark$
Allow ecf from part (f).
\% uncertainty in $g$
$=0.33+(2 \times 0.41)=1.15 \mathrm{~V}$
Allow ecf at each stage of calculation.
Uncertainty in $g$
$=10.0 \times 1.15 / 100=0.12 \mathrm{~m} \mathrm{~s}^{-2}$ or $0.1 \mathrm{~m} \mathrm{~s}^{-2} \checkmark$
Allow ecf from part (g).
(allow 1 or 2 sf only)
(Must have unit for 3rd mark).
(i) (a) Use spherical objects of different mass and determine mass with balance $\checkmark$

Annotate the script with the appropriate letter at the point where the mark has been achieved.
(b) Would need same diameter spherical objects for fair comparison (same air resistance etc) $\checkmark$
(c) Time spherical object falling through same height and compare times

Alternative for (c):
i.e. repeat whole of experiment, plot extracted values of $g$ against mass. Horizontal line expected, concluding acceleration same for different masses.

